

問1

(1)

$$Z_L = j\omega L = j \times 2 \times \pi \times f \times L = j \times 2 \times 3.14 \times 1 \times 10^3 \times 3 \times 10^{-3} = j18.84[\Omega]$$

$$Z_C = \frac{1}{j\omega C} = \frac{1}{j \times 2 \times \pi \times f \times C} = \frac{1}{j \times 2 \times 3.14 \times 1 \times 10^3 \times 30 \times 10^{-6}} = -j5.31[\Omega]$$

$$Z = Z_R + \frac{1}{\frac{1}{Z_L} + \frac{1}{Z_C}} = Z_R + \frac{Z_L Z_C}{Z_L + Z_C} = 10 + \frac{j18.84 \times (-j5.31)}{j18.84 + (-j5.31)} = 10 - j7.39[\Omega]$$

(2)

$$Z = \sqrt{10^2 + (-7.39)^2} \angle \tan^{-1}\left(\frac{-7.39}{10}\right) = 12.43 \angle -36.5^\circ [\Omega]$$

(3)

$$I = \frac{V}{Z} = \frac{10 \angle 20^\circ}{12.43 \angle -36.5^\circ} = \frac{10}{12.43} \angle 20^\circ - (-36.5^\circ) = 0.805 \angle 56.5^\circ [\text{V}]$$

(4)

$$V = IZ = 2 \angle 30^\circ \times 12.43 \angle -36.5^\circ = 2 \times 12.43 \angle 30^\circ + (-36.5^\circ) = 24.86 \angle -6.5^\circ [\text{V}]$$

問2

(1)

$$Z_1 = 10 \cos 30^\circ + j10 \sin 30^\circ = 8.66 + j5[\Omega]$$

$$Z_2 = 10 \cos 70^\circ + j10 \sin 70^\circ = 3.42 + j9.4[\Omega]$$

$$Z = Z_1 + Z_2 = 8.66 + j5 + 3.42 + j9.4 = 12.09 + j14.4[\Omega]$$

$$= \sqrt{12.09^2 + 14.4^2} \angle \tan^{-1}\left(\frac{14.4}{12.09}\right) = 18.8 \angle 50^\circ [\Omega]$$

(2)

$$I = \frac{V}{Z} = \frac{30 \angle -40^\circ}{18.8 \angle 50^\circ} = \frac{30}{18.8} \angle -40^\circ - 50^\circ = 1.6 \angle -90^\circ [\text{A}]$$

(3)

$$V = IZ = 3 \angle -40^\circ \times 18.8 \angle 50^\circ = 3 \times 18.8 \angle -40^\circ + 50^\circ = 56.4 \angle 10^\circ [\text{V}]$$

(4)

$$I = \frac{V}{Z} = \frac{30\angle -40^\circ}{18.8\angle 50^\circ} = \frac{30}{18.8}\angle -40^\circ - 50^\circ = 1.6\angle -90^\circ [\text{A}]$$

$$V_1 = IZ_1 = 1.6\angle 90^\circ \times 10\angle 30^\circ = 1.6 \times 10\angle 90^\circ + 30^\circ = 16\angle -60^\circ [\text{V}]$$

(5)

$$I = \frac{V}{Z} = \frac{30\angle -40^\circ}{18.8\angle 50^\circ} = \frac{30}{18.8}\angle -40^\circ - 50^\circ = 1.6\angle -90^\circ [\text{A}]$$

$$V_2 = IZ_2 = 1.6\angle -90^\circ \times 10\angle 70^\circ = 1.6 \times 10\angle -90^\circ + 70^\circ = 16\angle -20^\circ [\text{V}]$$

問3

(1)

$$Z_1 = 10 \cos 30^\circ + j10 \sin 30^\circ = 8.66 + j5 [\Omega]$$

$$Z_2 = 10 \cos 70^\circ + j10 \sin 70^\circ = 3.42 + j9.4 [\Omega]$$

$$Z = \frac{Z_1 Z_2}{Z_1 + Z_2} = \frac{(8.66 + j5) \times (3.42 + j9.4)}{8.66 + j5 + 3.42 + j9.4} = \frac{-17.38 + j98.5}{12.09 + j14.4} = \frac{(-17.38 + j98.5)(12.09 - j14.4)}{(12.09 + j14.4)(12.09 - j14.4)} = 3.42 + j4.08 [\Omega]$$

$$= \sqrt{3.42^2 + 4.08^2} \angle \tan^{-1}\left(\frac{4.08}{3.42}\right) = 5.32\angle 50^\circ [\Omega]$$

(2)

$$I = \frac{V}{Z} = \frac{30\angle -40^\circ}{5.32\angle 50^\circ} = \frac{30}{5.32}\angle -40^\circ - 50^\circ = 5.64\angle -90^\circ [\text{A}]$$

(3)

$$V = IZ = 3\angle -40^\circ \times 5.32\angle 50^\circ = 3 \times 5.32\angle -40^\circ + 50^\circ = 16.17\angle 10^\circ [\text{V}]$$