

問1

$$(1) Y_L = \frac{1}{j\omega L} = \frac{1}{j2\pi fL} = \frac{1}{j2 \times 3.14 \times 1 \times 10^3 \times 1 \times 10^{-3}} = \frac{1}{j6.28} = -j0.159[S]$$

$$Y_C = j\omega C = j2\pi fC = j2 \times 3.14 \times 1 \times 10^3 \times 10 \times 10^{-6} = j0.063[S]$$

$$Y = Y_L + Y_C = -j0.159 + j0.063 = -j0.096[S]$$

$$(2) Z = \frac{1}{Y} = \frac{1}{-j0.096} = j10.4 = 10.4 \angle 90^\circ [\Omega]$$

$$(3) I = \frac{V}{Z} = \frac{10 \angle 20^\circ}{10.4 \angle 90^\circ} = \frac{10}{10.28} \angle 20^\circ - (90^\circ) = 0.96 \angle -70^\circ$$

問2

$$(1) Y_{LR} = \frac{1}{j\omega L + R} = \frac{1}{j2\pi fL + R} = \frac{1}{j2 \times 3.14 \times 1 \times 10^3 \times 1 \times 10^{-3} + 1} = \frac{1}{j6.28 + 1} = 0.025 - j0.155[S]$$

$$Y_C = j\omega C = j2\pi fC = j2 \times 3.14 \times 1 \times 10^3 \times 10 \times 10^{-6} = j0.063[S]$$

$$Y = Y_L + Y_C = 0.025 - j0.155 + j0.063 = 0.025 - j0.092[S]$$

$$(2) Z = \frac{1}{Y} = \frac{1}{0.025 - j0.092} = 2.75 + j10.12 = 10.49 \angle 74.8^\circ [\Omega]$$

$$(3) I = \frac{V}{Z} = \frac{10 \angle 20^\circ}{10.49 \angle 74.8^\circ} = \frac{10}{10.28} \angle 20^\circ - (74.8^\circ) = 0.95 \angle -54.8^\circ$$

問3

$$(1) f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2 \times 3.14 \sqrt{1 \times 10^{-3} \times 10 \times 10^{-6}}} = 1592[\text{Hz}]$$

$$(2) Z = \infty[\Omega]$$

$$(3) I = \frac{V}{Z} = \frac{10 \angle 20^\circ}{\infty} = 0[A]$$

問4

(1) 合成アドミタンス Y は

$$Y = Y_{LR} + Y_C = \frac{1}{j\omega L + R} + j\omega C = \frac{(R - j\omega L)}{(R + j\omega L)(R - j\omega L)} + j\omega C = \frac{(R - j\omega L)}{R^2 + (\omega L)^2} + j\omega C$$
$$= \frac{R}{R^2 + (\omega L)^2} + j\left(\omega C - \frac{\omega L}{R^2 + (\omega L)^2}\right)$$

共振角周波数 ω_0 は虚部が 0 になる角周波数なので、

$$\omega_0 C - \frac{\omega_0 L}{R^2 + (\omega_0 L)^2} = 0$$

$$C = \frac{L}{R^2 + (\omega_0 L)^2}$$

$$R^2 + (\omega_0 L)^2 = \frac{L}{C}$$

$$(\omega_0 L)^2 = \frac{L}{C} - R^2$$

$$\omega_0^2 = \frac{1}{LC} - \frac{R^2}{L^2}$$

$$\omega_0 = \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$$

よって、共振周波数 f_0 は、

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$$

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}} = \frac{1}{2 \times 3.14} \sqrt{\frac{1}{1 \times 10^{-3} \times 10 \times 10^{-6}} - \frac{1^2}{(1 \times 10^{-3})^2}} = 1584 [\text{Hz}]$$

(2) 共振時は虚部が 0 なので、そのときのアドミタンス Y_0 は、先ほど求めた合成アドミタンスの実部である。

$$Y_0 = \frac{R}{R^2 + (\omega_0 L)^2} [S]$$

共振時のインピーダンス Z_0 は、その逆数なので、

$$Z_0 = \frac{1}{Y_0} = \frac{R^2 + (\omega_0 L)^2}{R} = \frac{R + (2\pi f_0 L)^2}{R} = \frac{1^2 + (2 \times 3.14 \times 1584 \times 1 \times 10^{-3})^2}{1^2} = 100 [\Omega]$$

$$(3) I = \frac{V}{Z} = \frac{10 \angle 20^\circ}{100 \angle 0^\circ} = 0.1 \angle 20^\circ [A]$$